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# Magnets that Meet Tracking Requirements for AHF

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# AHF Magnet Designs

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- **Dipole Magnet**

- $B = 0.15$  T at Injection (4 GeV)
- $B = 1.64$  T at Extraction (50 GeV)
- $L_{\text{eff}} = 6.87$  m
- Gap = 5.0 cm

- **Quadrupole Magnet**

- $G = 1.81$  T/m at Injection (4 GeV)
- $G = 18.5$  T/m at Extraction (50 GeV)
- $L_{\text{eff}} = 1.29$  m or 1.55 m
- Pole tip radius = 5.0 cm

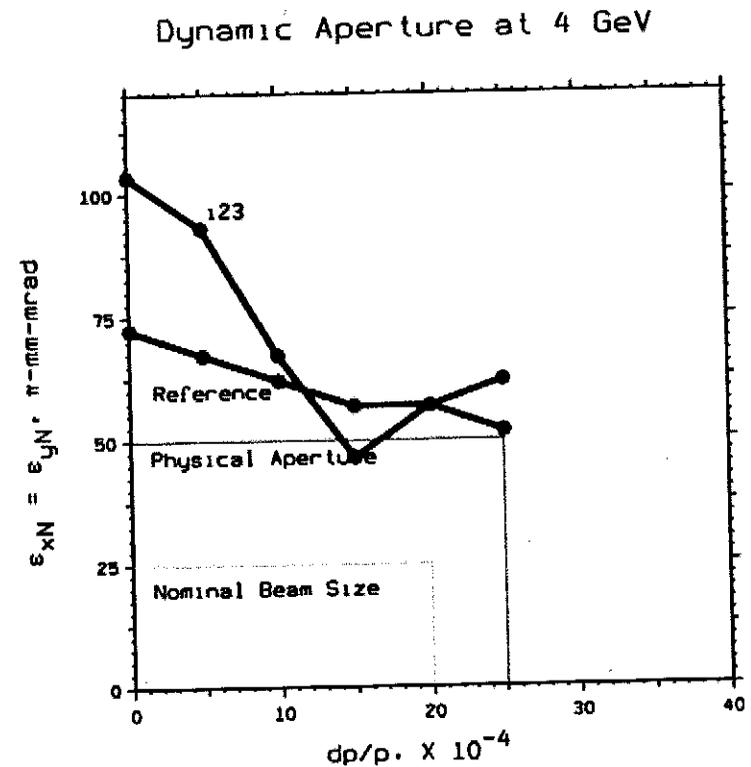
# AHF Magnet Design Selections

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- **Dipole Magnet**
  - **FNAL MI or SSC MEB Design (longer with more sagitta)**
  - **Procurement, fabrication and assembly based on FNAL MI**
  - **Meets AHF requirements**
  
- **Quadrupole Magnet**
  - **Initial tracking studies based on harmonics in FNAL MI**  
**Handbook shows dynamic aperture problems at injection**
  - **Performed analysis to better understand source of harmonics**
  - **Studied different quadrupole designs and measurements to determine reasonable requirements**
  - **Verified dynamic aperture with new requirements**

# Initial Studies of Dynamic Aperture

original			
(based on values in FNAL MI Handbook)			
Multipole Order	Coefficient	systematic	random
quadrupole	b2		24
sextupole	b3	-0.51	2.73
octupole	b4	1	1.02
decapole	b5	0.03	1.12
duodecapole	b6	-1.49	0.63
	14 b7	0.21	0.64
	16 b8	1.14	0.64
	18 b9	-0.19	0.12
	20 b10	-0.77	0.06
skew sextupole	a3	1.08	1.85
skew octupole	a4	-2.05	2.38
skew decapole	a5	-0.75	0.47
skew duodecapole	a6	0.43	0.7
	14 a7	0	0.44
	16 a8	0	0
	18 a9	-0.07	0.16
	20 a10	-0.12	0.07



- Dynamic aperture smaller than physical aperture
- Dipole random and systematic harmonics based on FMI magnet measurements
- Quadrupole random and systematic harmonics based on “old” magnet measurements of FNAL main ring

# HARMONICS CONVENTION

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- Normal -  $B_n$
- Skew -  $A_n$
- Dipole -  $n=1$
- Quadrupole -  $n=2$
- Expressed in Units of  $10^{-4} \Delta B_n/B_2$  at a radius of 2.54 cm

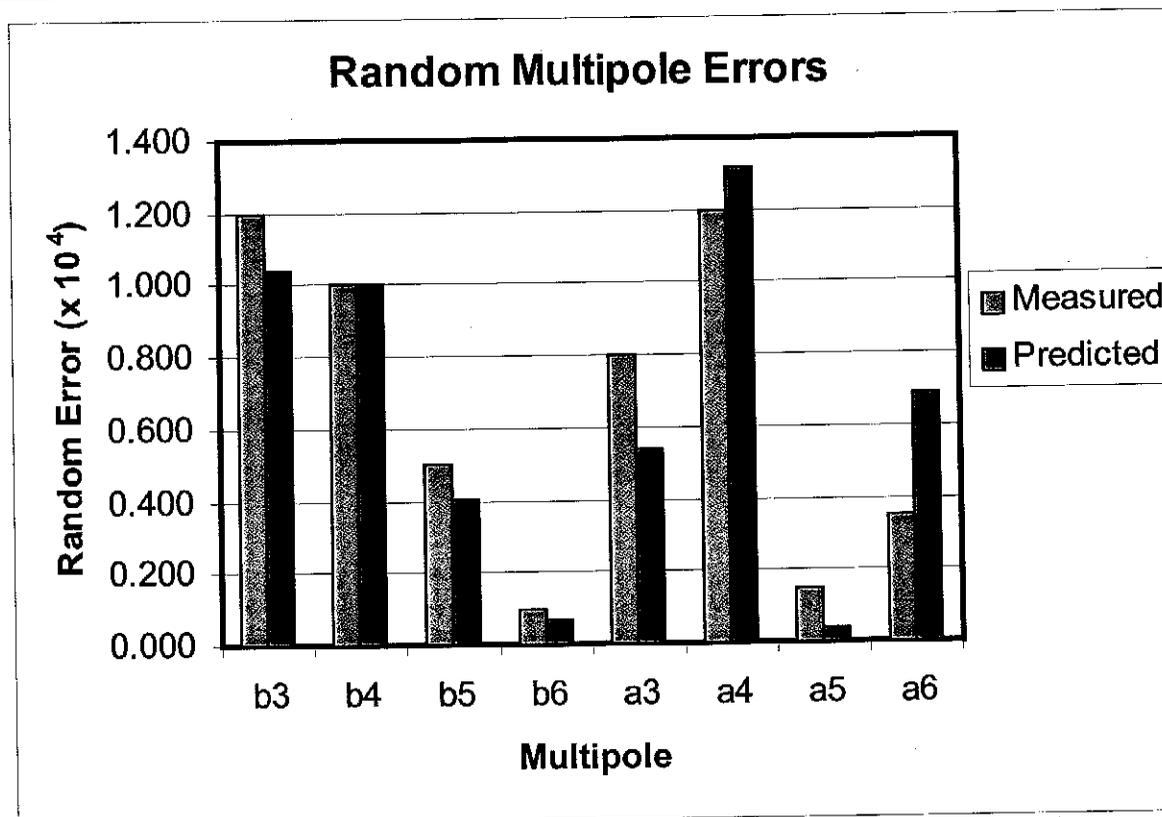
# Analysis of Quadrupole Magnet Harmonics for AHF

- **Analyze Quadruple Measurement Data for a variety of Magnets**
  - Better understanding of random errors
  - Look at assembly tolerances and errors
    - Coil proximity to pole
    - Gaps/tilts between half cores and quadrants
  - Determine “reasonably achievable” systematic and random errors
  - Add 30% margin and use result as “requirement”
- **Quadrupole Measurement Data**
  - FNAL MI Quads
  - ANL ALS Quads
  - LER Quads (SLAC PEP-II)
  - SQC Quads (FNAL Antiproton Accumulator)

## Analysis of Quadrupole Magnet Harmonics for AHF (cont)

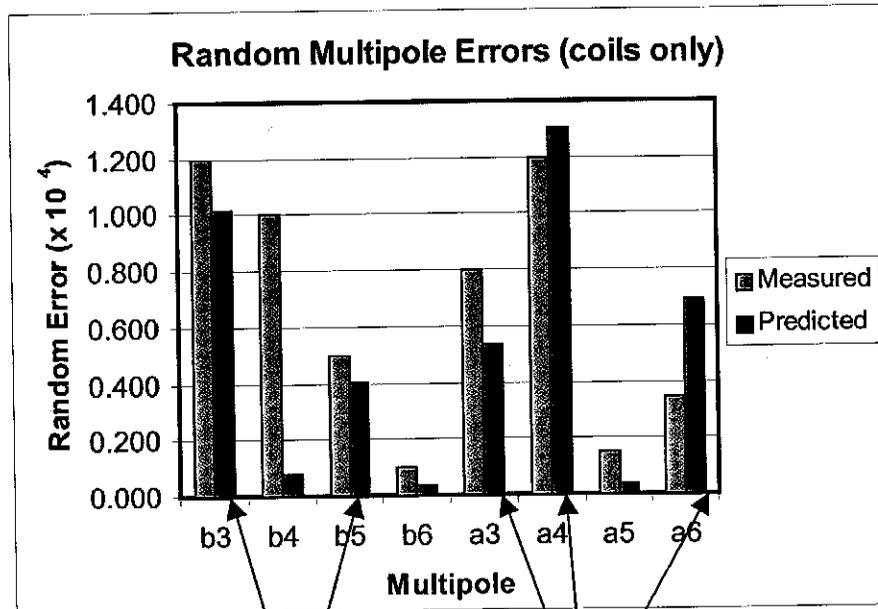
- **Analyze Recently Built IQC and IQD MI Quadruples**
  - **Analyze Measurement Data**
    - **Correlation between measured harmonics**
    - **Magnitude of Random Errors**
  - **Analyze MI Quadrupole with POISSON**
    - **Look at assembly tolerances and errors in 2D**
      - **Coil placement errors**
      - **Gaps between iron quadrants and half cores**
      - **Tilts between iron quadrants and half cores**
      - **Translation between iron mating surfaces**
      - **Stacking factor asymmetries**
  - **Compare simulated fabrication errors with measured random errors**
    - **They will have a distribution and a standard deviation**
    - **Can we predict the random multipole errors on the basis of the POISSON 2D models?**

# Good Agreement with Measured Random Errors

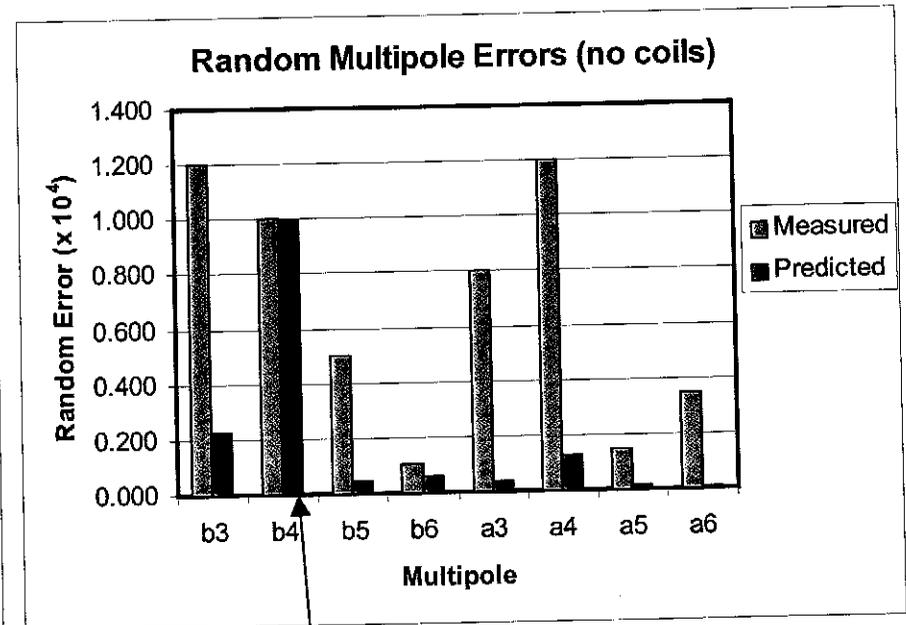


- Three main sources of random errors identified
  - Coil placement errors ( $\sigma = .018''$ )
  - Gaps between half cores ( $\sigma = .0011''$ )
  - Tilts between half cores ( $\sigma = .05$  mrad)

# Random errors are dominated by coil placement errors



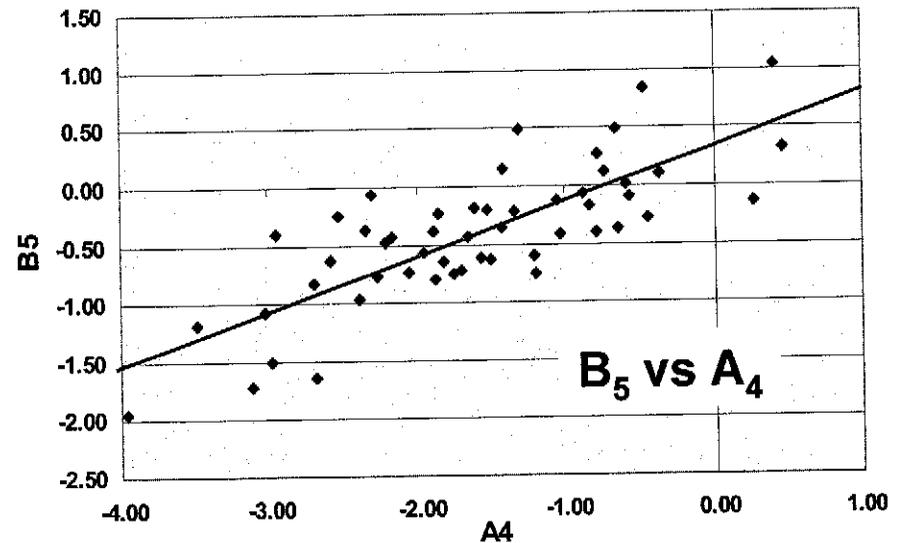
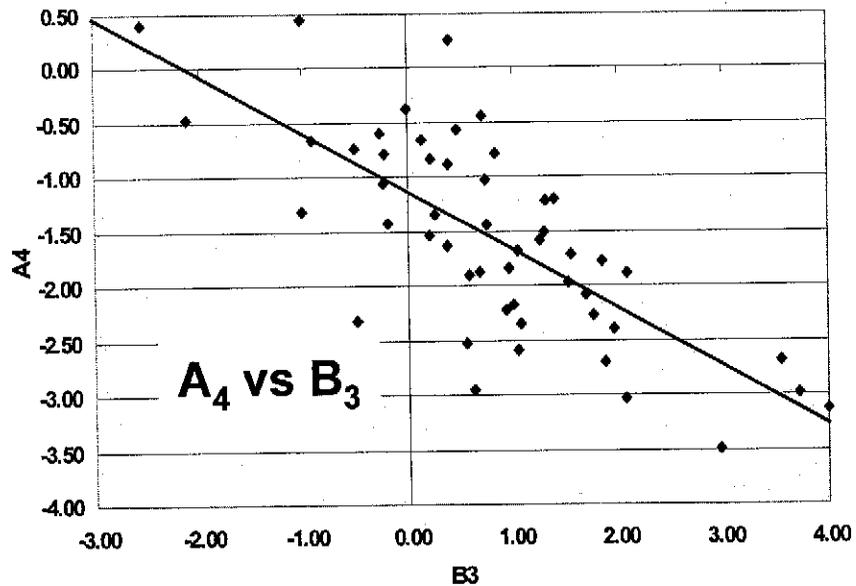
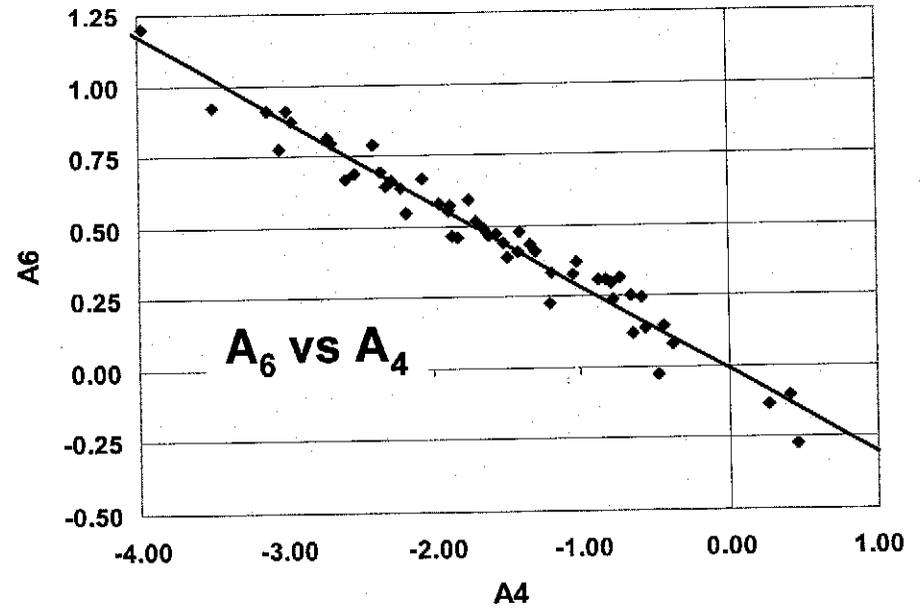
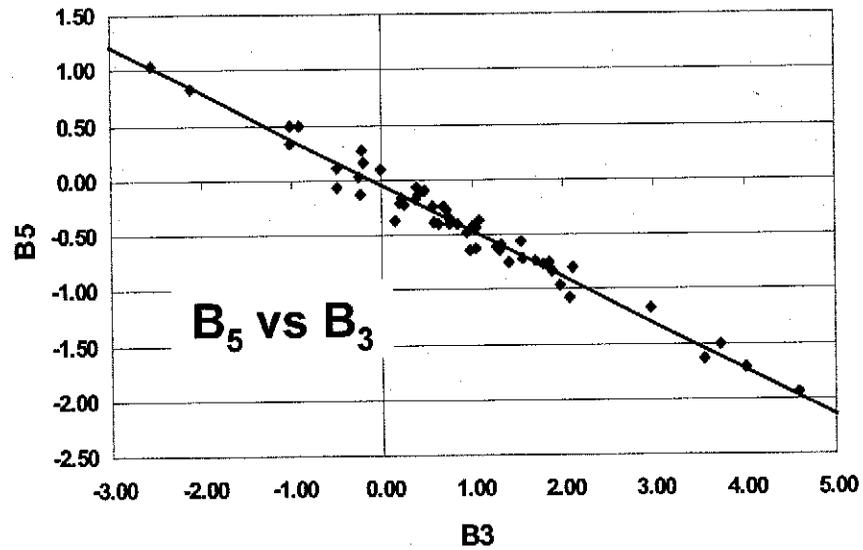
**Strong correlation with coil placement error**



**Strong correlation with iron mating surface gaps**

- Investigate correlation between measured harmonics to support analysis
- Look for correlation between  $B_3$ ,  $A_3$ ,  $A_4$ ,  $B_5$ ,  $A_6$

# Strong correlation observed for harmonics excited by coil placement errors (except $A_3$ )

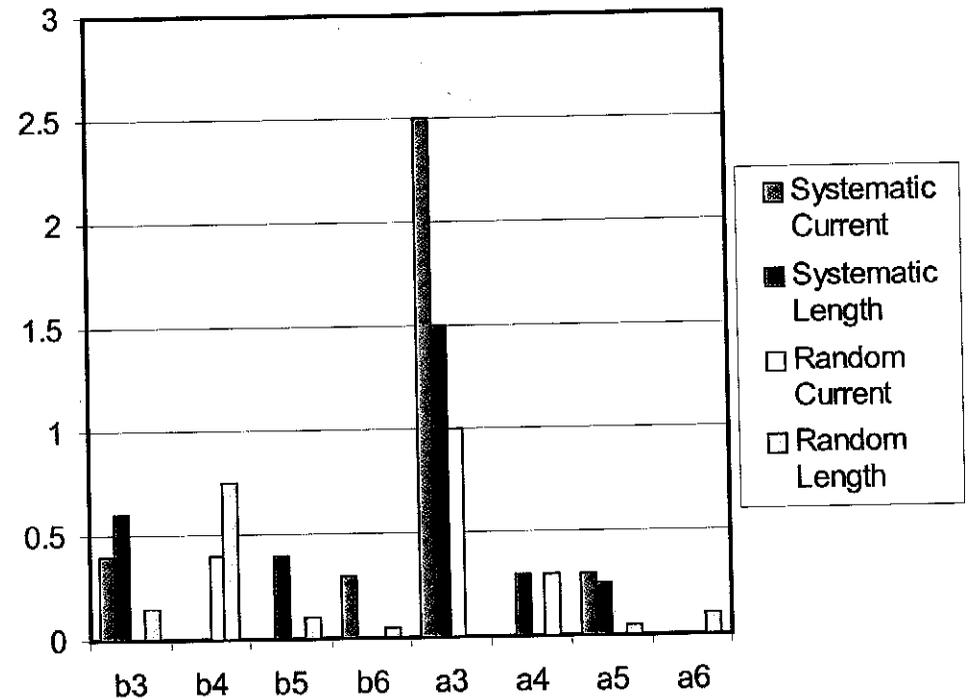
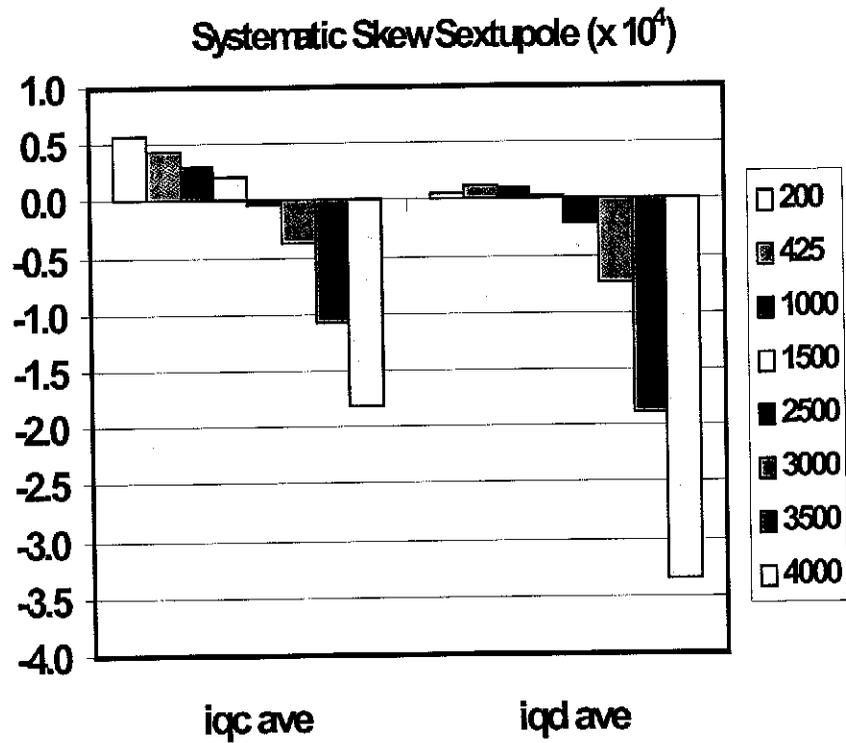


## Summary of Harmonics Analysis

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- **Most Random Errors can be Modeled as 2D Assembly Tolerances**
  - **Coil placement errors and proximity to pole tip can dominate errors**
  - **Random octupole ( $B_4$ ) caused by gaps and tilts between half cores**
    - **Systematic octupole is generally present**
  - **End effects not considered ( $A_3$ )**
    - **IQC and IQD have different lengths**
    - **Look at length and current dependence**

# Skew Sextupole ( $A_3$ ) shows Significant Length and Current Sensitivity



Skew sextupole field is dominated by end effects

# Compare Quadrupole Magnet Harmonics for SQC and LER

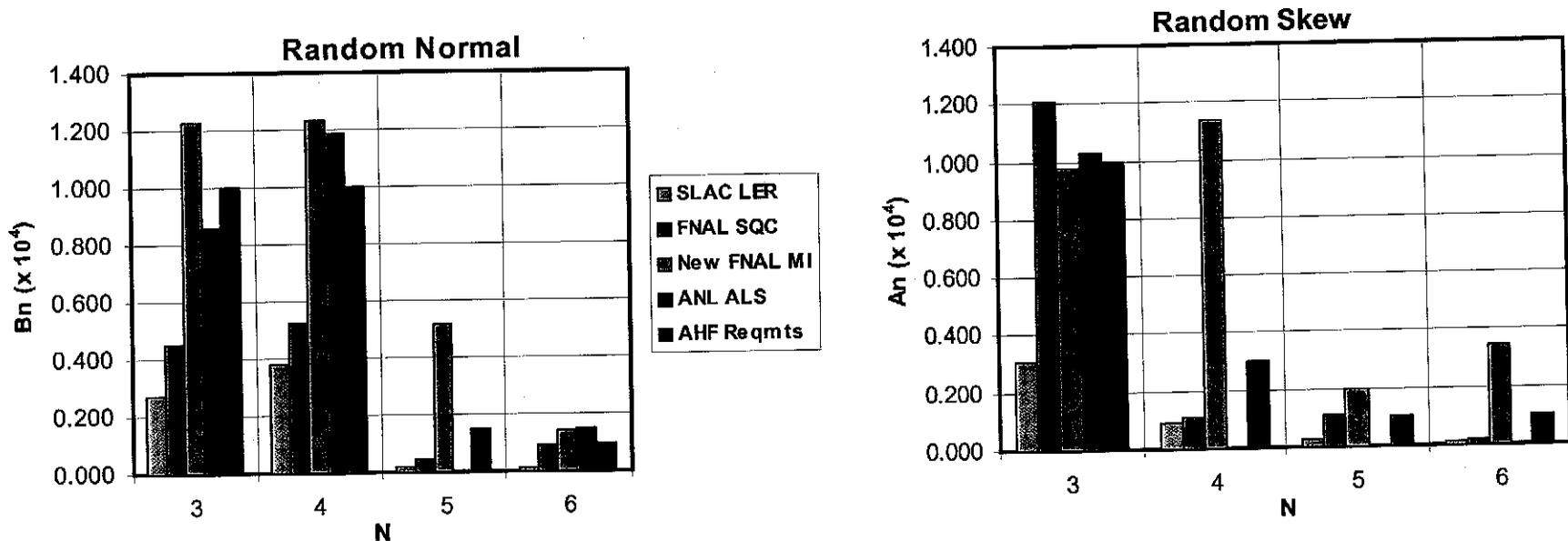
SQC Quadrupoles				
n	normal	normal	skew	skew
	systematic	random	systematic	random
3	-0.015	0.450	0.109	1.210
4	-1.090	0.520	-0.130	0.108
5	-0.006	0.043	-0.007	0.110
6	-0.170	0.089		0.020
9	0.001	0.003	0.001	0.004
10	0.030	0.012	-0.001	0.002
12	-0.003			

LER Quadrupoles				
n	normal	normal	skew	skew
	systematic	random	systematic	random
3	-0.034	0.273	-0.029	0.307
4	0.184	0.380	-0.005	0.091
5	0.004	0.022	0.006	0.025
6	0.339	0.013	-0.006	0.011
7		0.003		0.003
8		0.001		0.002
9		0.001		
10	-0.013			

- Harmonics above n=6 are very small
- Consider only sextupole through duodecapole harmonics

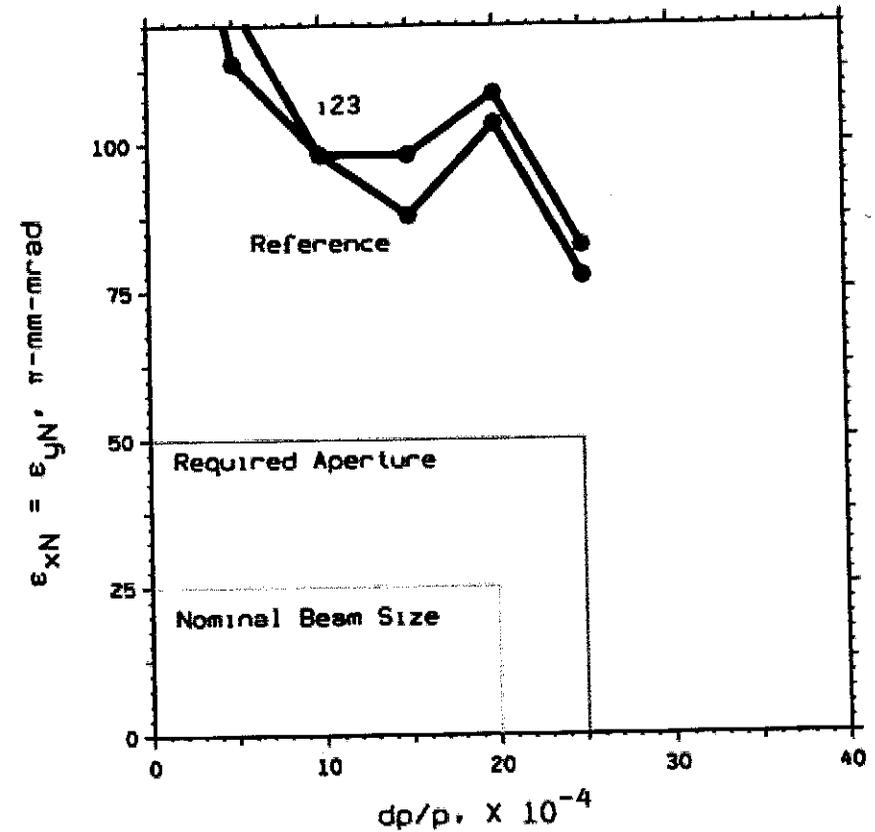
# Quadrupole Magnet Random Harmonics



- All above magnets provide a dynamic aperture larger than the physical aperture for AHF
- Sextupole and octupole random errors are the most significant
- Expect random errors to be factor of two worse than best magnets
- Add ~30% margin to define requirements
- FNAL MI magnets are almost twice as long as AHF quads

# AHF Quadrupole Magnet Harmonics Requirements and Tracking Results

AHF Quadrupole Magnet Harmonics Requirements			
Multipole Order	Coefficient	Systematic	Random
quadrupole	b2		12
sextupole	b3	0.2	1
octupole	b4	-0.5	1
decapole	b5	-0.1	0.15
duodecapole	b6	0.4	0.1
skew sextupole	a3	0.3	1
skew octupole	a4	0.1	0.3
skew decapole	a5	-0.1	0.1
skew duodecapole	a6	-0.1	0.1



Dynamic aperture is significantly larger than physical aperture

# AHF Quadrupole Magnet Design Considerations

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- **Avoid Sensitivity of Harmonics to Coil Placement Errors**
  - Move coils away from pole tip
  - Even number of coil layers - be careful with coil leads
- **Half Core vs Four Quadrant Construction**
  - Half core construction reduces sources of fabrication errors
  - Half core construction can restrict coil envelope
- **Presently Considering Two Designs**
  - SSC MEB scaled to 5.0 cm radius (quadrants)
  - SLAC LER (half core)
  - Both designs require modified coil package
  - Both designs can meet AHF requirements
- **Design Selection and Optimization in progress**

# Summary

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- **FMI or MEB dipoles adequate to maintain dynamic aperture**
- **Quadrupoles can be built to maintain dynamic aperture**
  - **Avoid coil placement problems**
  - **Considering SSC MEB or SLAC LER designs**
- **Tracking results based on new requirements show substantial margin for dynamic aperture**